

# Practical Attacks on Full-round FRIET

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**Abstract.** FRIET is a duplex-based authenticated encryption scheme proposed at EUROCRYPT 2020. It follows a novel design approach for built-in countermeasures against fault attacks. By a judicious choice of components, the designers propose the permutation FRIET-PC that can be used to build an authenticated encryption cipher denoted as FRIET-AE. And FRIET-AE provides a 128-bit security claim for integrity and confidentiality. In this paper, we research the propagation of pairs of differences and liner masks through the round function of FRIET-PC. For the full-round FRIET-PC, we can construct a differential distinguisher whose probability is 1 and a linear distinguisher whose absolute value of correlation is 1. Moreover, we use the differential distinguisher with probability 1 to construct a set consisting of valid tags and ciphertexts which are not created by legal users. This breaks FRIET-AE's security claim for integrity and confidentiality. As far as we know, this is the first practical attack that threatens the security of FRIET-AE.

**Keywords:** FRIET · Authenticated Encryption · Differential Attack · Linear Attack · Fault Injection

## 1 Introduction

Permutation-based cryptographic components are widely used in the design of ciphers. Firstly, permutations can be used in Sponge [BDPA08] mode to obtain hash functions. For example, KECCAK [BDPA11b] designed based on the permutation Keccak-f won the U.S. National Institute of Standards and Technology (NIST) Secure Hash Algorithm-3 (SHA3) competition in 2012. Secondly, permutations can be used in Even-Mansour [EM97] mode to get block ciphers, such as Simpira-EM [GM16]. Thirdly, permutations can be used in Duplex [BDPA11a] construction to design authenticated encryption (AE) ciphers. For example, ASCON [DEMSb] designed in this strategy was selected in the final portfolio of Competition for Authenticated Encryption: Security, Applicability and Robustness (CAESAR). Under this background, many cryptographic permutations are proposed, such as Alzette [BBdS<sup>+</sup>20], Gimli [BKL<sup>+</sup>17], Xoodoo [DHAK18], Frit [SBD<sup>+</sup>18], FRIET [SBD<sup>+</sup>20], etc.

For their good security and implementation advantages, permutation-based cryptographic components are also widely used in the design of lightweight ciphers. In March 2021, NIST Lightweight Cryptography Project (LWC) announced the ten finalists. It should be noted that 6 of 10 are permutation based. They are ASCON [DEMSa], Elephant [BCDM], ISAP [DEM<sup>+</sup>], Photo-Beetle [BCD<sup>+</sup>], SPARKLE [BBdS<sup>+</sup>] and Xoodyak [DHP<sup>+</sup>]. Because lightweight ciphers are often used in constrained environments (constraints on energy, area and memory size), they may be exposed to side channel attacks. In order to mitigate such attacks, at EUROCRYPT 2020, Simon *et al.* proposed a novel design method for ciphers with efficient fault-detecting implementations and a concrete authenticated encryption



**Table 1:** The comparison of the distinguishers for FRIET-PC

*Type	Round	†Probability/Correlation/Data	Reference
LC	7	$2^{-29}$	[SBD <sup>+</sup> 20]
	8	$2^{-40}$	[SBD <sup>+</sup> 20]
	* <i>R</i>	1 or -1	Sect. 3.1
R-DL	8	$2^{-17.81}$	[LSL21]
	9	$2^{-29.81}$	[LSL21]
	13	$2^{-117.81}$	[LSL21]
IC	13	$2^{-31}$	[ISS <sup>+</sup> 21]
	15	$2^{-63}$	[ISS <sup>+</sup> 21]
	17	$2^{-127}$	[ISS <sup>+</sup> 21]
	30	$2^{-383}$	[ISS <sup>+</sup> 21]
DC	6	$2^{-59}$	[SBD <sup>+</sup> 20]
	9	$2^{-20.04}$	[ISS <sup>+</sup> 21]
	* <i>R</i>	1	Sect. 3.2

\* R-DL denotes rotational differential-linear distinguisher. LC denotes linear distinguisher. DC denotes differential distinguisher. IC denotes integral distinguisher.

† The DC is showed with probability. LC/DL/R-DL are showed with correlation. IC is showed with data.

\* *R* means that the differential or linear distinguisher is valid for any-round FRIET-PC.

scheme called FRIET [SBD<sup>+</sup>20]. And they designed new cryptographic permutations called FRIET-PC and FRIET-P for the implementation of FRIET.

An earlier version of FRIET-PC is called Frit [SBD<sup>+</sup>18] proposed by the same authors. It wasn't long before Dobraunig *et al.* [DEMS19] studied the algebraic properties of Frit and gave a key recovery attack against the full-round Frit-EM (the block cipher constructed by Frit in Even-Mansour mode). Then, Qin *et al.* [QDJZ19] gave some key-recovery attacks on the round-reduced Frit used in duplex authenticated encryption mode. By taking these attacks into account, a new permutation called FRIET-PC was designed. The designers evaluated the security of FRIET-PC against algebraic attack, slide attack, invariant subspace attack, non-linear invariant attack, differential attack, linear attack, etc. For example, by researching the properties of trail with low-weight input differences and linear masks, they obtained a 6-round differential trail with probability  $2^{-59}$  and an 8-round linear trail with correlation  $2^{-80}$ . At EUROCRYPT 2021, Liu *et al.* [LSL21] constructed a 12-round rotational differential-linear distinguisher with correlation  $2^{-117.81}$ . Then, Ito *et al.* [ISS<sup>+</sup>21] evaluated the security of FRIET-PC against bit-wise cryptanalysis including rotational attack, bit-wise differential attack and integral attack. It should be noted that the above attacks do not threaten the security of FRIET-PC.

## 1.1 Our Contributions

FRIET-PC adopts the AND-Rotation-XOR construction. And the only nonlinear operation in FRIET-PC is bitwise AND. By fixing the differential probability and linear correlation of AND operation, we research the propagation of differences and linear masks through the round function of FRIET-PC. For any-round FRIET-PC, we construct a differential distinguisher whose probability is 1 and a linear distinguisher whose absolute value of correlation is 1. The comparison with the previous results is shown in Table 1.

Moreover, when FRIET-PC is used in FRIET, we get an authenticated encryption cipher denoted as FRIET-AE. And FRIET-AE provides a 128-bit security claim for

integrity and confidentiality. Using the above differential distinguisher with probability 1, we can practically construct a set consisting of valid tags and ciphertexts which are not created by legal users. This breaks the claims for integrity and confidentiality of FRIET-AE. Therefore, the design of permutation FRIET-PC has defects.

## 1.2 Outline

This paper is organized as follows: Sect. 2 introduces differential and linear cryptanalysis and briefly describes the specification of FRIET permutation. In Sect. 3, we propose the differential and linear distinguishers for the full-round FRIET-PC. In Sect. 4, we give the practical attacks on the full-round FRIET-AE. Sect. 5 concludes the paper.

## 2 Preliminaries

### 2.1 Notations

Notations used in this paper are defined in Table 2.

**Table 2:** Notations used in this paper

$\mathbb{F}_2$	The finite field $\{0, 1\}$
$x \in \mathbb{F}_2^n$	An $n$ -bit vector
$x[i]$	The $i$ -th bit of $x$
$x \oplus y$	Bitwise XOR of $x$ and $y$
$\bar{x}$	Bitwise NOT of $x$
$x \vee y$	Bitwise OR of $x$ and $y$
$x \wedge y$	Bitwise AND of $x$ and $y$
$x \cdot y$	The inner product of $x$ and $y$
$x  y$	The concatenation of $x$ and $y$
$x \ll r$	Shift $x$ to the left by $r$ bits
$x \lll r$	Rotation of $x$ to the left by $r$ bits
$x \ggg r$	Rotation of $x$ to the right by $r$ bits
$wt(x)$	The hamming weight of $x$
$\lceil c \rceil$	The nearest integer greater than or equal to $c$
$\lfloor c \rfloor$	The nearest integer smaller than or equal to $c$
$\mathbf{0}_n$	An $n$ -bit vector with all entries equal 0
$\mathbf{1}_n$	An $n$ -bit vector with all entries equal 1

### 2.2 Differential and Linear Cryptanalysis

Differential cryptanalysis [BS90] and linear cryptanalysis [Mat93] are two powerful methods which have been widely used in the security analysis of many symmetric ciphers.

**Definition 1. (Differential [BS90]).** For a vectorial boolean function  $f : \mathbb{F}_2^n \rightarrow \mathbb{F}_2^m$ , let  $\alpha \in \mathbb{F}_2^n$  and  $\beta \in \mathbb{F}_2^m$  be the input and output differences of  $f$ . Then, the differential probability of  $[\alpha, \beta]$  over  $f$  is defined as:

$$Pr[\alpha \rightarrow \beta] = 2^{-n} \#\{x \in \mathbb{F}_2^n : f(x) \oplus f(x \oplus \alpha) = \beta\},$$

where  $\#\{x \in \mathbb{F}_2^n : f(x) \oplus f(x \oplus \alpha) = \beta\}$  is the number of  $x$  satisfying  $f(x) \oplus f(x \oplus \alpha) = \beta$ .

**Definition 2. (Linear Approximation [Mat93]).** For a vectorial boolean function  $f : \mathbb{F}_2^n \rightarrow \mathbb{F}_2^m$ , let  $\alpha \in \mathbb{F}_2^n$  and  $\beta \in \mathbb{F}_2^m$  be the input and output linear masks of  $f$ . Then, the correlation of the linear approximation  $(\alpha, \beta)$  over  $f$  is defined as

$$\text{Cor}(\alpha, \beta) = 2^{-n+1} \#\{x \in \mathbb{F}_2^n : \alpha \cdot x \oplus \beta \cdot f(x) = 0\} - 1,$$

where  $\#\{x \in \mathbb{F}_2^n : \alpha \cdot x \oplus \beta \cdot f(x) = 0\}$  is the number of  $x$  satisfying  $\alpha \cdot x \oplus \beta \cdot f(x) = 0$ .

Based on the above definitions, the trivial differential and linear approximation properties of basic operations (XOR, Branching, XOR-Constant) are introduced in [BS90, Mat93]. Here, we only introduce the differential and linear approximation properties of AND operation which will be used in this paper.

**Differential Property 1 (AND) [SBD<sup>+</sup>20].** Let  $z = f(x, y)$  be an AND function, where  $x \in \mathbb{F}_2^n$  and  $y \in \mathbb{F}_2^n$  are the input variables, and the output variable  $z$  is calculated as  $z = x \wedge y$ . Then,

$$\text{Pr}[\alpha || \beta \rightarrow \gamma] = \begin{cases} 2^{-wt(\alpha \vee \beta)}, & \text{if } \bar{\alpha} \wedge \bar{\beta} \wedge \gamma = \mathbf{0}_n, \\ 0, & \text{otherwise,} \end{cases}$$

where  $\alpha || \beta \in \mathbb{F}_2^{2n}$  and  $\gamma \in \mathbb{F}_2^n$  are the differences of  $x || y$  and  $z$ , respectively.

**Linear Property 1 (AND) [SBD<sup>+</sup>20].** Let  $z = f(x, y)$  be an AND function, where  $x \in \mathbb{F}_2^n$  and  $y \in \mathbb{F}_2^n$  are the input variables, and the output variable  $z$  is calculated as  $z = x \wedge y$ . Then,

$$\text{Cor}(\alpha || \beta, \gamma) = \begin{cases} 2^{-wt(\gamma)}, & \text{if } \gamma \vee (\bar{\alpha} \wedge \bar{\beta}) = \mathbf{1}_n, \\ 0, & \text{otherwise,} \end{cases}$$

where  $\alpha || \beta \in \mathbb{F}_2^{2n}$  and  $\gamma \in \mathbb{F}_2^n$  are the linear masks of  $x || y$  and  $z$ , respectively.

In order to apply differential (linear) cryptanalysis, cryptanalysts have to build a pair of differences (linear masks) for each round of a cipher, such that the output difference (linear mask) of a round matches the input difference (linear mask) of the next round. The differential probability (linear correlation) of the full-round cipher is computed by multiplying the differential probabilities (linear correlations) of each round. And we call a pair of differences (linear masks) valid when its differential probability (linear correlation) is nonzero. If a cipher behaves differently from a random cipher for differential (linear) cryptanalysis, this can be used to build a distinguishing or even a key-recovery attack.

### 2.3 Description of the Round Function of FRIET

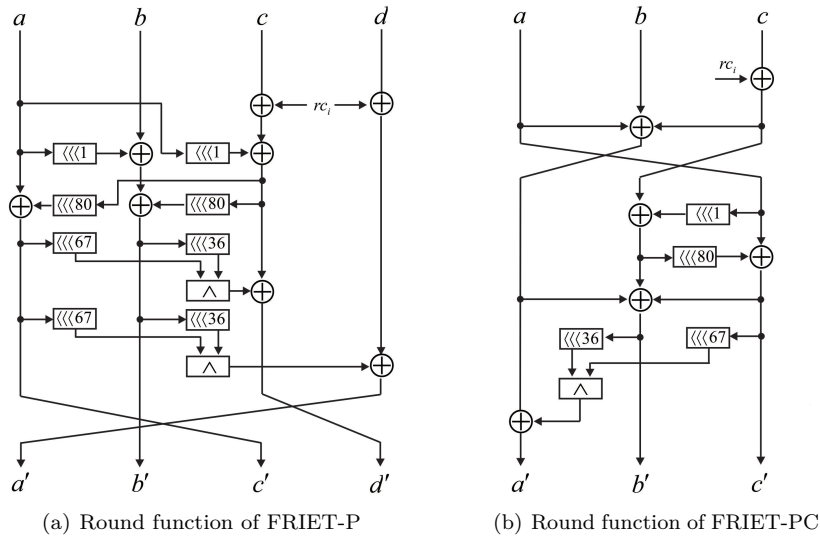
FRIET [SBD<sup>+</sup>20] is an authenticated encryption scheme with built-in fault detection mechanisms proposed by Simon *et al.* at EUROCRYPT 2020. Its fault detection ability comes from its underlying permutation, which is designed based on the so-called code embedding approach. The core permutation FRIET-P employed in FRIET operates on 4 limbs  $(a, b, c, d) \in \mathbb{F}_2^{4 \times 128}$ . The permutation FRIET-P is an iterative design with its round function  $f_{rc_i}(a, b, c, d)$  visualized in the left part of Figure 1, where  $rc_i$  is the round constant for the  $i$ -th round listed in Table 3.

By design, the round function  $(a', b', c', d') = f(a, b, c, d)$  has slice-wise code-abiding property. Mathematically, it means that  $a \oplus b \oplus c = d$  implies  $a' \oplus b' \oplus c' = d'$ . Thus, the permutation FRIET-P =  $f_{rc_{23}} \circ f_{rc_{22}} \circ \dots \circ f_{rc_0}$  also has this property. Consequently, faults will be detected if output does not have code-abiding property when the input state has code-abiding property. If we ignore the limb  $d$  of FRIET-P, we will obtain a new

**Table 3:** Round constants  $rc_i$  in hexadecimal notation

$i$	0	1	2	3	4	5
$rc_i$	0x1111	0x11100000	0x1101	0x10100000	0x101	0x10110000
$i$	6	7	8	9	10	11
$rc_i$	0x110	0x11000000	0x1001	0x100000	0x100	0x10000000
$i$	12	13	14	15	16	17
$rc_i$	0x1	0x110000	0x111	0x11110000	0x1110	0x11010000
$i$	18	19	20	21	22	23
$rc_i$	0x1010	0x1010000	0x1011	0x1100000	0x1100	0x10010000

permutation FRIET-PC visualized in the right part of Figure 1. Since a distinguisher for the permutation FRIET-PC directly translates to a distinguisher for FRIET-P, we focus on the permutation FRIET-PC. And we describe the procedure of FRIET-PC permutation as shown in Algorithm 1.

**Figure 1:** The round function of FRIET [SBD<sup>+</sup>20]

### 3 Differential and Linear Distinguishers for the Full-Round FRIET-PC

FRIET-PC only has four operations: Rotation, XOR, XOR-Constant and AND. Bitwise AND is the only nonlinear operation in FRIET-PC. If we can effectively control the propagations of differences and linear masks through bitwise AND operation, we can obtain pairs of differences with high probabilities and linear masks with high correlations.

#### 3.1 A Differential Distinguisher for the Full-Round FRIET-PC

Because Rotation, XOR, XOR-Constant are all linear operations, the differential probability of a valid pair of differences for these three operations is 1. By **Differential Property 1 (AND)**, the differential probability of a valid pair of differences for bitwise AND operation

**Algorithm 1** FRIET-PC [SBD<sup>+</sup>20]**Input:** The three limbs  $a, b, c \in \mathbb{F}_2^{128}$  and the round constants  $rc_i, 0 \leq i \leq 23$ **Output:**  $(a', b', c') \leftarrow \text{FRIET-PC}(a, b, c)$ 


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1: for  $i$  from 0 to 23 do
2:    $c \leftarrow c \oplus rc_i$ 
3:    $(a, b, c) \leftarrow (a \oplus b \oplus c, c, a)$ 
4:    $b \leftarrow b \oplus (c \lll 1)$ 
5:    $c \leftarrow c \oplus (b \lll 80)$ 
6:    $(a, b, c) \leftarrow (a, a \oplus b \oplus c, c)$ 
7:    $a \leftarrow a \oplus ((b \lll 36) \wedge (c \lll 67))$ 
8: end for
9: return  $(a, b, c)$ 

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is determined by  $wt(\alpha \vee \beta)$ , where  $\alpha$  and  $\beta$  are the input differences of the bitwise AND operation. By controlling the value of  $wt(\alpha \vee \beta)$  effectively, we may obtain a pair of differences with high probability.

**Lemma 1.** *The differential probability of  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma')$  for the  $i$ -th round function  $(a', b', c') = \text{FRIET-PC}_i(a, b, c)$  of FRIET-PC is 1 if and only if*

$$\begin{cases} \alpha' = \alpha \oplus \beta \oplus \gamma, \\ \alpha \oplus (\alpha \lll 1) \oplus \beta = \mathbf{0}_{128}, \\ \alpha \oplus (\alpha \lll 81) \oplus (\gamma \lll 80) = \mathbf{0}_{128}, \\ \beta' = \mathbf{0}_{128}, \\ \gamma' = \mathbf{0}_{128}. \end{cases} \quad (1)$$

*Proof.* On one hand, if the differential probability of  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma')$  is 1, according to **Differential Property 1 (AND)**, both the two input differences of AND operation should be  $\mathbf{0}_n$ . Because the two input variables vector of AND are  $b' \lll 36$  and  $c' \lll 67$ , we have  $\beta' = \mathbf{0}_{128}$ ,  $\gamma' = \mathbf{0}_{128}$  and the output difference of  $(b' \lll 36) \wedge (c' \lll 67)$  should also be  $\mathbf{0}_{128}$ . And due to

$$\begin{cases} a' = a \oplus b \oplus c \oplus rc_i \oplus ((b' \lll 36) \wedge (c' \lll 67)), \\ b' = a \oplus (a \lll 1) \oplus b \oplus c', \\ c' = a \oplus (a \lll 81) \oplus ((c \oplus rc_i) \lll 80), \end{cases}$$

we have

$$\begin{cases} \alpha' = \alpha \oplus \beta \oplus \gamma, \\ \beta' = \alpha \oplus (\alpha \lll 1) \oplus \beta = \mathbf{0}_{128}, \\ \gamma' = \alpha \oplus (\alpha \lll 81) \oplus (\gamma \lll 80) = \mathbf{0}_{128}. \end{cases}$$

The necessity is proved.

On the other hand, if a pair of differences  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma')$  satisfies the Eq. (1), its differential probabilities through all the basic operations (Rotation, XOR, XOR-Constant, AND) in the round function of FRIET-PC is 1. Thus, the differential probability of  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma')$  is 1. The sufficiency is proved.  $\square$

Next, we will research the differential property of the 2-round FRIET-PC.

**Lemma 2.** *The differential probability of a nonzero differential  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma') \rightarrow (\alpha'', \beta'', \gamma'')$  for the 2-round FRIET-PC is 1 if and only if*

$$\begin{cases} \alpha = \alpha' = \alpha'' = \mathbf{1}_{128}, \\ \beta = \beta' = \beta'' = \mathbf{0}_{128}, \\ \gamma = \gamma' = \gamma'' = \mathbf{0}_{128}. \end{cases} \quad (2)$$

*Proof.* According to Lemma 1, the differential probability of  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma') \rightarrow (\alpha'', \beta'', \gamma'')$  is 1 if and only if

$$\alpha' = \alpha \oplus \beta \oplus \gamma, \quad (3)$$

$$\alpha \oplus (\alpha \lll 1) \oplus \beta = \mathbf{0}_{128}, \quad (4)$$

$$\alpha \oplus (\alpha \lll 81) \oplus (\gamma \lll 80) = \mathbf{0}_{128}, \quad (5)$$

$$\beta' = \mathbf{0}_{128}, \quad (6)$$

$$\gamma' = \mathbf{0}_{128}, \quad (7)$$

$$\alpha'' = \alpha' \oplus \beta' \oplus \gamma', \quad (8)$$

$$\alpha' \oplus (\alpha' \lll 1) \oplus \beta' = \mathbf{0}_{128}, \quad (9)$$

$$\alpha' \oplus (\alpha' \lll 81) \oplus (\gamma' \lll 80) = \mathbf{0}_{128}, \quad (10)$$

$$\beta'' = \mathbf{0}_{128}, \quad (11)$$

$$\gamma'' = \mathbf{0}_{128}. \quad (12)$$

On one hand, from Eq. (6) and Eq. (9), we have  $\alpha' = \alpha' \lll 1$ . The only two values of  $\alpha'$  satisfying  $\alpha' = \alpha' \lll 1$  are  $\alpha' = \mathbf{0}_{128}$  and  $\alpha' = \mathbf{1}_{128}$ .

If  $\alpha' = \mathbf{0}_{128}$ , we have  $(\alpha', \beta', \gamma') = \mathbf{0}_{3 \times 128}$ . Because the round function of FRIET-PC is bijective, it contradicts with that  $(\alpha, \beta, \gamma) \rightarrow (\alpha', \beta', \gamma') \rightarrow (\alpha'', \beta'', \gamma'')$  is a nonzero differential.

If  $\alpha' = \mathbf{1}_{128}$ , from Eq. (6), (7) and (8), we have  $\alpha'' = \mathbf{1}_{128}$ . According to Eq. (4) and Eq. (5) we have

$$((\alpha \oplus (\alpha \lll 81) \oplus (\gamma \lll 80)) \ggg 80) \oplus \alpha \oplus (\alpha \lll 1) \oplus \beta = (\mathbf{0}_{128} \ggg 80) \oplus \mathbf{0}_{128}$$

Combining with Eq. (3), we have

$$(\alpha \ggg 80) = \alpha' = \mathbf{1}_{128}.$$

Thus,  $\alpha = \mathbf{1}_{128}$ . Substituting the value  $\alpha = \mathbf{1}_{128}$  into Eq. (4) and Eq. (5), we have  $\beta = \mathbf{0}_{128}$  and  $\gamma = \mathbf{0}_{128}$ . The necessity is proved.

On the other hand, the nonzero difference  $(\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128}) \rightarrow (\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128}) \rightarrow (\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$  satisfies all the Eq. (3-12). The sufficiency is proved.  $\square$

Based on Lemma 2, we can get the following corollary easily.

**Corollary 1.** For  $n$ -round FRIET-PC,  $(\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128}) \rightarrow \cdots \rightarrow (\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$  is the only nonzero differential with probability 1, where  $n \geq 2$ .

Thus, we obtain a differential distinguisher with probability 1 for the full-round FRIET-PC. In order to help readers understand the differential distinguisher better, we show the propagation of it through 1-round FRIET-PC in the left part of Figure 2.

### 3.2 A Linear Distinguisher for the Full-Round FRIET-PC

Because Rotation, XOR, XOR-Constant are all linear operations, the linear correlation of a valid pair of linear masks for these three operations is 1 or -1. By **Linear Property 1 (AND)**, the linear correlation of a valid pair of linear masks for bitwise AND operation is determined by  $wt(\gamma)$ , where  $\gamma$  is the output linear mask of the bitwise AND operation. By controlling the value of  $wt(\gamma)$  effectively, we may obtain pairs of linear masks with high correlations.

**Lemma 3.** Let  $\Gamma_{in} = (\alpha, \beta, \gamma)$  and  $\Gamma_{out} = (\alpha', \beta', \gamma')$  be the input and output linear masks of the  $i$ -th round function  $(a', b', c') = \text{FRIET-PC}_i(a, b, c)$ . The absolute value of correlation  $\text{Cor}(\Gamma_{in}, \Gamma_{out})$  is 1 if and only if

$$\begin{cases} \alpha' = \mathbf{0}_{128}, \\ \alpha \oplus (\beta' \ggg 1) \oplus \gamma' \oplus ((\beta' \oplus \gamma') \ggg 81) = \mathbf{0}_{128}, \\ \beta \oplus \beta' = \mathbf{0}_{128}, \\ \gamma \oplus ((\beta' \oplus \gamma') \ggg 80) = \mathbf{0}_{128}. \end{cases} \quad (13)$$

*Proof.* By the round function of FRIET-PC, we have

$$\begin{cases} a' = a \oplus b \oplus c \oplus rc_i \oplus ((b' \lll 36) \wedge (c' \lll 67)) \\ b' = (a \lll 1) \oplus b \oplus (a \lll 81) \oplus ((c \oplus rc_i) \lll 80), \\ c' = a \oplus (a \lll 81) \oplus ((c \oplus rc_i) \lll 80). \end{cases}$$

On one hand, if the absolute value of  $\text{Cor}(\Gamma_{in}, \Gamma_{out})$  is 1. According to **Linear Property 1 (AND)**, the input linear mask and output linear mask of AND operation should be  $\mathbf{0}_{128} \parallel \mathbf{0}_{128}$  and  $\mathbf{0}_{128}$ , respectively. Because  $((b' \lll 36) \wedge (c' \lll 67))$  only appear in  $a'$ , we have  $\alpha' = 0$ . Then,

$$\begin{aligned} \Gamma_{in} \cdot (a, b, c) \oplus \Gamma_{out} \cdot (a', b', c') &= \alpha \cdot a \oplus \beta \cdot b \oplus \gamma \cdot c \oplus \alpha' \cdot a' \oplus \beta' \cdot b' \oplus \gamma' \cdot c' \\ &= \alpha \cdot a \oplus \beta' \cdot (a \lll 1) \oplus \gamma' \cdot a \oplus (\beta' \oplus \gamma') \cdot (a \lll 81) \\ &\quad \oplus (\beta \oplus \beta') \cdot b \oplus \gamma \cdot c \oplus (\beta' \oplus \gamma') \cdot (c \lll 80) \\ &\quad \oplus (\beta' \oplus \gamma') \cdot (rc_i \lll 80) \\ &= (\alpha \oplus (\beta' \ggg 1) \oplus \gamma' \oplus ((\beta' \oplus \gamma') \ggg 81)) \cdot a \\ &\quad \oplus (\beta \oplus \beta') \cdot b \oplus (\gamma \oplus ((\beta' \oplus \gamma') \ggg 80)) \cdot c \\ &\quad \oplus (\beta' \oplus \gamma') \cdot (rc_i \lll 80). \end{aligned}$$

We know that the above  $\Gamma_{in} \cdot (a, b, c) \oplus \Gamma_{out} \cdot (a', b', c')$  is a linear function. Thus, if  $|\text{Cor}(\Gamma_{in}, \Gamma_{out})| = 1$ , we have

$$\begin{cases} \alpha' = \mathbf{0}_{128}, \\ \alpha \oplus (\beta' \ggg 1) \oplus \gamma' \oplus ((\beta' \oplus \gamma') \ggg 81) = \mathbf{0}_{128}, \\ \beta \oplus \beta' = \mathbf{0}_{128}, \\ \gamma \oplus ((\beta' \oplus \gamma') \ggg 80) = \mathbf{0}_{128}. \end{cases}$$

The necessity is proved.

On the other hand, if the input linear mask  $(\alpha, \beta, \gamma)$  and output linear mask  $(\alpha', \beta', \gamma')$  satisfy Eq. (13), the linear correlations through all the basic operations (Rotation, XOR, XOR-Constant, AND) in the round function of FRIET-PC is 1 or -1. Thus, the absolute value of the linear correlation is 1. The sufficiency is proved.  $\square$

According to Lemma 3, we obtain the following corollary.

**Corollary 2.** For the input linear mask  $\Gamma_{in} = (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128})$  and output linear mask  $\Gamma_{out} = (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128})$ , the absolute value of correlation  $\text{Cor}(\Gamma_{in}, \Gamma_{out})$  for  $n$ -round FRIET-PC is 1, where  $n \geq 1$ .

*Proof.* Because  $\Gamma_{in} = (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128})$  and  $\Gamma_{out} = (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128})$  satisfy Eq. (13). The absolute value of correlation  $\text{Cor}(\Gamma_{in}, \Gamma_{out})$  for 1-round FRIET-PC is 1. By applying the propagation of linear masks  $(\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128}) \rightarrow (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{1}_{128})$  iteratively, the absolute value of correlation  $\text{Cor}(\Gamma_{in}, \Gamma_{out})$  for  $n$ -round FRIET-PC is 1.  $\square$

Thus, we obtain a linear distinguisher whose absolute value of correlation is 1 for full-round FRIET-PC. In order to help readers understand the linear distinguisher better, we show the propagation of it through 1-round FRIET-PC in the right part of Figure 2.



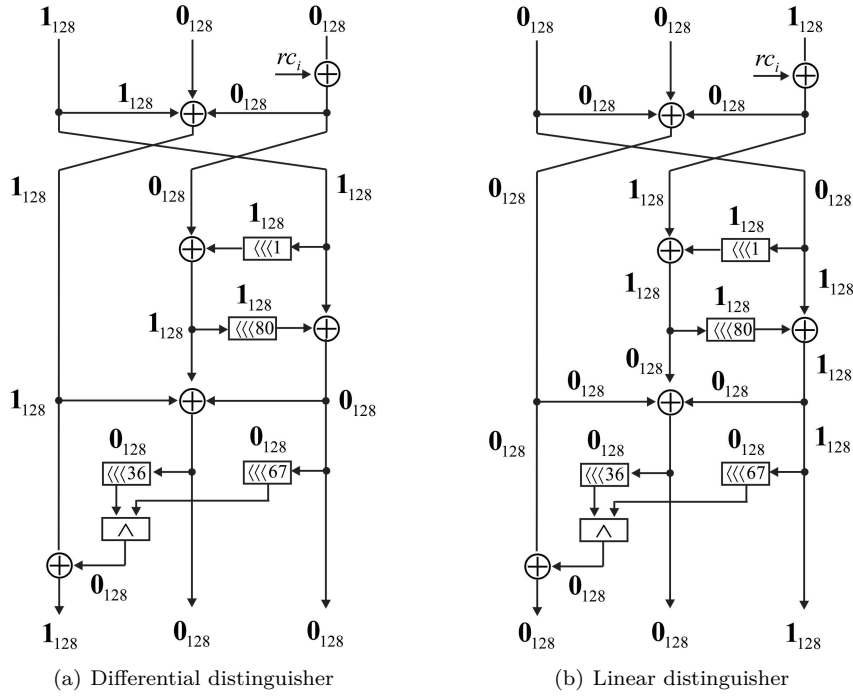


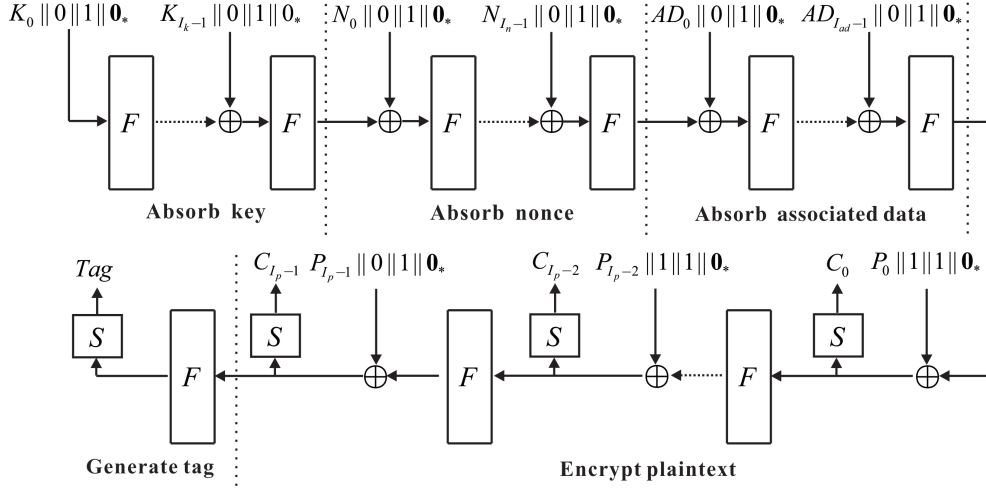
Figure 2: The differential and linear distinguishers of 1-round FRIET-PC

## 4 Practical Attacks on the Full-Round FRIET-AE

### 4.1 Description of FRIET-AE

When FRIET-P is used in FRIET authenticated encryption scheme, FRIET-AE is obtained. It is based on duplex construction and its mode SpongeWrap [BDPA11a], but some modifications are made. FRIET-AE limits the key length to 160 bits and takes tag length and block length as 128 bits. Let  $Tag \in \mathbb{F}_2^{128}$  and  $C$  be the tag and ciphertexts which are generated by  $FRIET-AE(K, N, AD, P)$ , where  $K$  is the key,  $N$  is the nonce,  $AD$  is the associate data,  $P$  is the plaintexts. Because the block length is 128 bits, all the input data are split into 128-bit blocks and the last block may be shorter. Take  $K$  for an example, let  $|K|$  denote the bit length of  $K$ . The number of blocks of  $K$  is  $I_k = \left\lceil \frac{|K|}{128} \right\rceil$ , denoted as  $K = K_{I_k-1} || \dots || K_1 || K_0$ . And the number of blocks of  $K$  whose length is 128 bits is  $J_k = \left\lfloor \frac{|K|}{128} \right\rfloor$ . In the same way, we can get the values of  $I_n, I_{ad}, I_p$  and  $J_n, J_{ad}, J_p$  for  $N, AD, P$ , respectively. In order to describe the FRIET-AE more concisely, without affecting the correctness, we assume that all the plaintext blocks are 128 bits. That is  $I_p = J_p$ .

In this paper, we do not study its fault-resistance ability. Thus, the input and output of permutation FRIET-PC are 3 limbs (384 bits), denoted as  $(a', b', c') = F(a, b, c)$ . The function of getting the ciphertext or tag by squeezing the state is denoted as  $a = S(a, b, c)$ . The detailed encryption procedure of FRIET-AE is showed in Figure 3 and Algorithm 2, where  $\mathbf{0}_*$  means adding a bit vector whose binary entries are all 0 until the length of the entire vector reaches 384 bits.



**Figure 3:** The encryption procedure of FRIET-AE [SBD<sup>+</sup>20]

---

**Algorithm 2** *FRIET-AE* ( $K, N, AD, P$ ) [SBD<sup>+</sup>20]

---

**Input:**  $K, N, AD, P$

**Output:**  $C, Tag$

- 1:  $s = \mathbf{0}_{384}$  ▷ The initial value of state
  - 2: **for**  $i_k$  from 0 to  $I_k - 1$  **do** ▷  $K = K_{I_k-1} || \dots || K_1 || K_0$
  - 3:      $s = F(K_{i_k} || 0 || 1 || \mathbf{0}_* \oplus s)$
  - 4: **end for**
  - 5: **for**  $i_n$  from 0 to  $I_n - 1$  **do** ▷  $N = N_{I_n-1} || \dots || N_1 || N_0$
  - 6:      $s = F(N_{i_n} || 0 || 1 || \mathbf{0}_* \oplus s)$
  - 7: **end for**
  - 8: **for**  $i_{ad}$  from 0 to  $I_{ad} - 1$  **do** ▷  $AD = AD_{I_{ad}-1} || \dots || AD_1 || AD_0$
  - 9:      $s = F(AD_{i_{ad}} || 0 || 1 || \mathbf{0}_* \oplus s)$
  - 10: **end for**
  - 11: **for**  $i_p$  from 0 to  $I_p - 2$  **do** ▷  $P = P_{I_p-1} || \dots || P_1 || P_0$
  - 12:      $s = s \oplus P_{i_p} || 1 || 1 || \mathbf{0}_*$
  - 13:      $C_{i_p} = S(s)$
  - 14:      $s = F(s)$
  - 15: **end for**
  - 16:  $s = s \oplus P_{I_p-1} || 0 || 1 || \mathbf{0}_*$  ▷ The encryption of the last block of plaintext is different
  - 17:  $C_{I_p-1} = S(s)$
  - 18:  $s = F(s)$
  - 19:  $Tag = S(s)$  ▷ Generate *Tag*
  - 20: **return** ( $C = C_{I_p-1} || \dots || C_1 || C_0, Tag$ )
- 

## 4.2 The Method of Breaking Full-round FRIET-AE

Under the assumption that adversaries respect the nonce requirement for the diversifier and do not get access to deciphered ciphertexts of cryptograms with an invalid tag, FRIET-AE claims a 128-bit security of integrity and confidentiality. If adversaries can construct a new cryptogram data which has not ever been created by legal users and the cryptogram data can be successfully decrypted by a legal user, the integrity is broken. If keystream (keyed duplex output) can be predicted or a cryptogram can be decrypted by adversaries, the confidentiality is broken. By using the differential distinguisher with probability 1 in Corollary 1, we design an algorithm to generate a set consisting of cryptograms data which

are not created by legal users. We illustrate the whole framework in Algorithm 3.

---

**Algorithm 3** *Attack* ( $K, N, AD, P, C, Tag$ )

---

**Input:** ( $K, N, AD, P, C, Tag$ )

**Output:** A set  $\Omega$  consisting of valid cryptograms data

```

1: Initialize  $\Omega = \emptyset$ ,  $flag = 0$ ,  $J_k = \lfloor \frac{|K|}{128} \rfloor$ ,  $J_n = \lfloor \frac{|N|}{128} \rfloor$ ,  $J_{ad} = \lfloor \frac{|AD|}{128} \rfloor$ ,  $J_p = \lfloor \frac{|P|}{128} \rfloor$ 
2: for  $u_k \in \mathbb{F}_2^{J_k}$ ,  $u_n \in \mathbb{F}_2^{J_n}$ ,  $u_{ad} \in \mathbb{F}_2^{J_{ad}}$ ,  $u_p \in \mathbb{F}_2^{J_p}$  do
3:   if  $u_k = \mathbf{0}_{J_k}$  and  $u_n = \mathbf{0}_{J_n}$  and  $u_{ad} = \mathbf{0}_{J_{ad}}$  and  $u_p = \mathbf{0}_{J_p}$  then
4:     continue
5:   end if
6:   Let  $K' = K$ ,  $N' = N$ ,  $AD' = AD$ ,  $P' = P$ ,  $C' = C$ ,  $Tag' = Tag$ 
7:   for  $j_k$  for 0 to  $J_k - 1$  do
8:     if  $u_k[j_k] = 1$  then
9:        $K' = K' \oplus (\mathbf{1}_{128} \ll (j_k \times 128))$ 
10:       $flag = flag \oplus 1$ 
11:     end if
12:   end for
13:   for  $j_n$  from 0 to  $J_n - 1$  do
14:     if  $u_n[j_n] = 1$  then
15:        $N' = N' \oplus (\mathbf{1}_{128} \ll (j_n \times 128))$ 
16:        $flag = flag \oplus 1$ 
17:     end if
18:   end for
19:   for  $j_{ad}$  from 0 to  $J_{ad} - 1$  do
20:     if  $u_{ad}[j_{ad}] = 1$  then
21:        $AD' = AD' \oplus (\mathbf{1}_{128} \ll (j_{ad} \times 128))$ 
22:        $flag = flag \oplus 1$ 
23:     end if
24:   end for
25:   for  $j_p$  from 0 to  $J_p - 1$  do
26:     if  $u_p[j_p] = 1$  then
27:        $P' = P' \oplus (\mathbf{1}_{128} \ll (j_p \times 128))$ 
28:        $flag = flag \oplus 1$ 
29:     end if
30:     if  $flag = 1$  then
31:        $C' = C' \oplus (\mathbf{1}_{128} \ll (j_p \times 128))$ 
32:     end if
33:   end for
34:   if  $flag = 1$  then
35:      $Tag' = Tag' \oplus \mathbf{1}_{128}$ 
36:   end if
37:    $\Omega = \Omega \cup \{(K', N', AD', P', C', Tag')\}$ 
38: end for
39: return  $\Omega$ 

```

---

We explain **Algorithm 3** line by line:

**Input:** A cryptogram data ( $K, N, AD, P, C, Tag$ ) is needed, where the  $Tag \in \mathbb{F}_2^{128}$  and ciphertexts  $C$  are generated by **Algorithm 2** *FRIET-AE* ( $K, N, AD, P$ ).

**Output:** The output set  $\Omega$  is composed of other valid cryptogram data different from ( $K, N, AD, P, C, Tag$ ).

**Line 1:** Let  $\Omega$  be empty set.  $flag = 0$  means that the difference of current state is  $(\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$ , while  $flag = 1$  means the difference is  $(\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$ . Same as the

definition in Section 4.1,  $J_k, J_n, J_{ad}, J_p$  denotes the number of 128-bit blocks of  $K, N, AD, P$ , respectively.

**Line 2–36:** The bit vectors  $u_k, u_n, u_{ad}, u_p$  are used to indicate whether the difference  $\mathbf{1}_{128}$  is introduced to some blocks of  $K, N, AD, P$ , respectively. Take  $K$  for example,  $u_k[j_k] = 1$  means the difference between blocks  $K_{j_k}$  and  $K'_{j_k}$  is  $\mathbf{1}_{128}$  and  $u_k[j_k] = 0$  means the difference is  $\mathbf{0}_{128}$ . Because the generated cryptogram data should be different from the input cryptogram data  $(K, N, AD, P, C, Tag)$ , **Line 3** is added. According to Section 3.1, both the differential probabilities of  $(\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128}) \rightarrow (\mathbf{0}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$  and  $(\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128}) \rightarrow (\mathbf{1}_{128}, \mathbf{0}_{128}, \mathbf{0}_{128})$  over the full-round FRIET-PC are 1. Thus, the value of  $K'$  and current difference of state can be obtained by **Line 9-10**. In the same way, we can get the values of  $N', AD', C', Tag'$ .

**Line 37:** All the generated cryptogram data are added into the set  $\Omega$ .

All the cryptogram data  $(K', N', AD', P', C', Tag') \in \Omega$  have valid tags and ciphertexts which are not created by legal users. It should be noted that they belong to different attack conditions. We will have a classified discussion.

**Related-Key Attack.** According to Algorithm 3, we only introduce difference of the form  $\mathbf{1}_{128}||\mathbf{0}_{128}||\mathbf{0}_{128}$  to the internal state. When there is difference in  $K$ , the number of elements in the set  $\Omega$  is  $(2^{J_k} - 1) \times 2^{J_n} \times 2^{J_{ad}} \times 2^{J_p}$ .

**Single-Key Attack.** If there is no difference in  $K$ , under the condition that nonce cannot be reused, we must introduce differences into  $N$ . The number of elements in the set  $\Omega$  is  $(2^{J_n} - 1) \times 2^{J_{ad}} \times 2^{J_p}$ . If adversaries have the ability of reusing nonce, the number of elements in the set  $\Omega$  is  $2^{J_n} \times 2^{J_{ad}} \times 2^{J_p} - 1$ .

According to the above analysis, we can construct valid tags and ciphertexts which are not created by legal users. And the single-key attack without reusing nonce fully complies with the security assumption of FRIET-AE. This breaks the integrity and confidentiality security claims. And our attack can be conducted in practical time.

## 5 Conclusions

In this paper, differential and linear distinguishers for the full-round FRIET-PC are proposed. Using the differential distinguisher with probability 1, we proposed an algorithm which can generate a set consisting of valid tags and ciphertexts which are not created by legal users. This breaks the integrity and confidentiality security claims of FRIET-AE. It should be noted that our attack does not recover the secret key of FRIET-AE. How to give a key-recovery attack needs further research.

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